

# Implementation of Characteristic Mode Decomposition and the Source Concept

Miloslav Čapek<sup>1</sup>   Lukáš Jelínek<sup>1</sup>  
& AToM team<sup>2</sup>

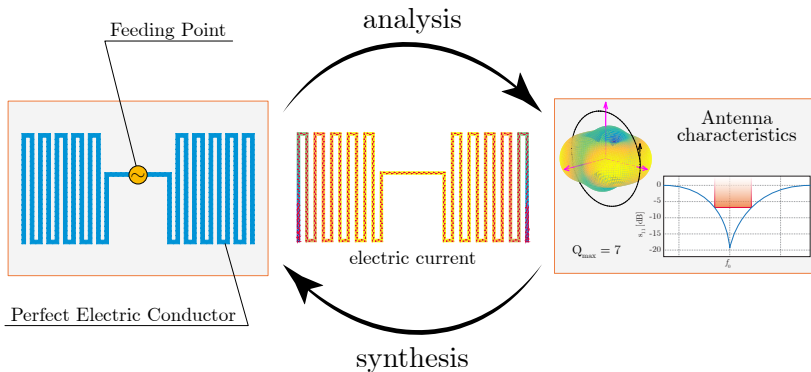
<sup>1</sup>Department of Electromagnetic Field  
CTU in Prague, Czech Republic  
`miloslav.capek@fel.cvut.cz`

Lund, Sweden  
November 12, 2015

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<sup>2</sup>Please, see [antennatoolbox.com/about-us](http://antennatoolbox.com/about-us). The results are based on the collaboration of all members.

- 1 Introduction
- 2 Source Concept
  - What is the source concept?
  - Selected applications of the source concept
  - Requirements
- 3 Characteristic mode decomposition
- 4 About AToM
- 5 AToM's Architecture
  - AToM – Closer Investigation
  - AToM's – Features
- 6 Integration into Visual CEM (ESI Group)



Antenna analysis  $\times$  antenna synthesis.

# AToM: Antenna Toolbox For Matlab

„Antenna source concept” – New approach to antenna design.



EM project **AToM (Antenna Toolbox For Matlab)**  
started from September 2014.



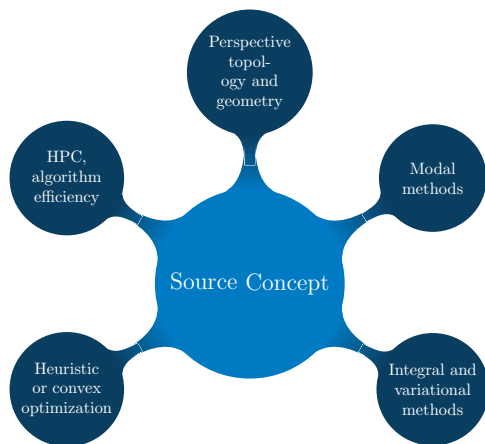
Logo of the AToM project.

The main idea behind the AToM toolbox is to develop new package that will be able to:

- ▶ utilize the source concept features
- ▶ handle with data from third party software
- ▶ accept other codes from the community
- ▶ make it possible the fast-prototyping of advanced antenna designs

# Source Concept

What is actually the Source Concept?



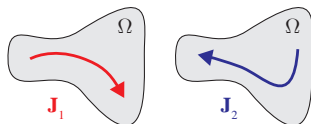
Sketch of main fields of the source concept.

It can be observed that ...

- ▶ an antenna is completely represented by a source current,
- ▶ all parameters can be inferred from a source current,
- ▶ any proper int.-diff. operator can be decomposed into modes,
- ▶ spatial decomposition of current is possible.

# Source Concept

Applications: Characteristic Modes



Modes  $\mathbf{J}_1$  and  $\mathbf{J}_2$  are depicted.

$$\mathbf{J} = \sum_{m=1}^M \frac{\langle \mathbf{J}_m, \mathbf{E}^i \rangle}{1 + j\lambda_m} \mathbf{J}_m$$

- ▶ characteristic mode (CM) decomposition<sup>3</sup>

$$\mathcal{X}\mathbf{J} = \lambda\mathcal{R}\mathbf{J} \quad (1)$$

- other useful decomposition

$$\mathbf{J} = \sum_m \gamma_m \mathbf{J}_m \quad (2)$$

- ▶ CMs are excellent for pattern synthesis or feeding network synthesis<sup>4</sup>

<sup>3</sup>R. F. Harrington and J. R. Mautz. "Theory of Characteristic Modes for Conducting Bodies". In: *IEEE Trans. Antennas Propag.* 19.5 (1971), pp. 622–628. DOI: 10.1109/TAP.1971.1139999

<sup>4</sup>R. F. Harrington and J. R. Mautz. "Pattern Synthesis for Loaded N-Port Scatterers". In: *IEEE Trans. Antennas Propag.* 22.2 (1974), pp. 184–190. DOI: 10.1109/TAP.1974.1140785

# Source Concept

Applications: Structural Decomposition



Division of  $\Omega$  into two parts.

$$\mathbf{J} = \bigcup_{k=1}^K \mathbf{J}_k$$

- ▶ similar to structural decomposition in mechanical engineering
- ▶ to decide what part of a radiator stores significant portion of energy / radiates well<sup>5</sup>
- ▶ excellent for synthesis of reflect arrays<sup>6</sup>
- ▶ combination with CM: sub-structure modes<sup>7</sup>

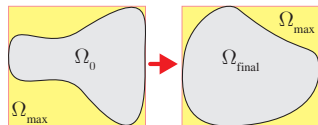
<sup>5</sup>M. Capek et al. “The Measurable Q Factor and Observable Energies of Radiating Structures”. In: *IEEE Trans. Antennas Propag.* 62.1 (2014), pp. 311–318. DOI: [10.1109/TAP.2013.2287519](https://doi.org/10.1109/TAP.2013.2287519)

<sup>6</sup>J. Ethier. “Antenna Shape Synthesis Using Characteristic Mode Concepts”. PhD thesis. University of Ottawa, 2012

<sup>7</sup>J. L. T. Ethier and D.A. McNamara. “Sub-structure characteristic mode concept for antenna shape synthesis”. In: *Electronics Letters* 48.9 (2012), pp. 471–472. ISSN: 0013-5194. DOI: [10.1049/el.2012.0392](https://doi.org/10.1049/el.2012.0392)

# Source Concept

Applications: Optimization



Optimization of antenna's shape.

single-objective optim.:

$$\{y_j\} = \min_{\{x_i\}} \mathcal{F}(\mathbf{J})$$

multi-objective optim.:

$$\{y_j\} = \min_{\{x_i\}} \{\mathcal{F}_j(\mathbf{J})\}$$

- ▶ both single- and multi-objective optimization can be utilized in order to obtain best antenna performance
- ▶ many objectives can be subjects of convex optimization<sup>8</sup>
  - $\mathcal{F}(\mathbf{J}, \mathbf{J})$  has to be positive semi-definite<sup>9</sup>
  - convex optimization does not result in specific design, only minimizes given convex function

<sup>8</sup>M. Gustafsson and S. Nordebo. "Optimal antenna currents for Q, superdirectivity, and radiation patterns using convex optimization". In: *IEEE Trans. Antennas Propag.* 61.3 (2013), pp. 1109–1118. doi: 10.1109/TAP.2012.2227656

<sup>9</sup>S. Boyd and L. Vandenberghe. *Convex Optimization*. Cambridge University Press, 2004



# Source Concept

Applications: Advanced Post-processing



Feeding network synthesis.

$$\beta_{m,n} = \Re \{ \alpha_m \alpha_n^* \}$$

where:

$$\lambda_m = \frac{\langle \mathbf{J}_m, \mathbf{E}^i \rangle}{1 + j\lambda_m}$$

- ▶ any antenna parameter can be defined by functional containing current(s)
- ▶ recently derived:
  - radiation efficiency without IBC<sup>10</sup>
  - measurable  $Q_Z$  factor<sup>11</sup>
  - energies for sub-wavelength radiators<sup>12</sup> ( $ka < 1$ )
  - no matter if modal / structural / total current is substituted

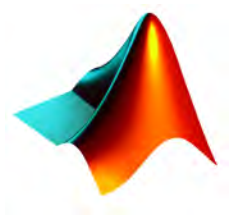
<sup>10</sup>M. Capek, J. Eichler, and P. Hazdra. “Evaluation of Radiation Efficiency from Characteristic Currents”. In: *IET Microw. Antennas Propag.* 9.1 (2015), pp. 10–15. DOI: [10.1049/iet-map.2013.0473](https://doi.org/10.1049/iet-map.2013.0473)

<sup>11</sup>M. Capek et al. “The Measurable Q Factor and Observable Energies of Radiating Structures”. In: *IEEE Trans. Antennas Propag.* 62.1 (2014), pp. 311–318. DOI: [10.1109/TAP.2013.2287519](https://doi.org/10.1109/TAP.2013.2287519)

<sup>12</sup>G. A. E. Vandenbosch. “Reactive Energies, Impedance, and Q Factor of Radiating Structures”. In: *IEEE Trans. Antennas Propag.* 58.4 (2010), pp. 1112–1127. DOI: [10.1109/TAP.2010.2041166](https://doi.org/10.1109/TAP.2010.2041166)

# Source Concept

Requirements: Fast-prototyping Environment



MathWorks MATLAB logo.

- ▶ up to now, there is no commercial package that completely implements techniques mentioned above
- ▶ however, scientists develop and utilize their own codes
  - the codes are mainly written in Matlab<sup>13</sup>

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<sup>13</sup>The MathWorks. *The Matlab*. 2015. URL: [www.mathworks.com](http://www.mathworks.com)

# Why Matlab?



## Pros

- ▶ high-definition language
  - excellent for fast-prototyping
  - many built-in functions are embedded
- ▶ new functionality can easily be published<sup>14</sup>
- ▶ maybe other...

## Cons

- ▶ still not fast as e.g. C
  - and to be efficient, Matlab needs very good programming skill
- ▶ not open-source
- ▶ to make standalone application is a nightmare
- ▶ maybe other...

- ▶ What is your opinion??

<sup>14</sup>[www.mathworks.com/matlabcentral/fileexchange](http://www.mathworks.com/matlabcentral/fileexchange)

# Source Concept

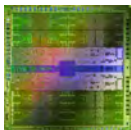
Requirements: Computational Resources



CPU

×

GPU




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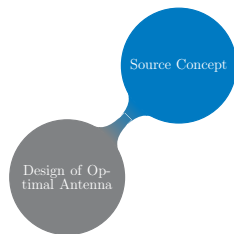
maybe FPGA in the future?

- ▶ advanced post-processing and optimization need high-performance computers<sup>15</sup>
  - HPC techniques
- ▶ depending on the nature of the problem
  - CPU can be employed in parallel / distributive mode
  - GPU can be employed
- ▶ Matlab fully supports CPU and GPU acceleration
  - implicit acceleration (matrix multiplication, fft,...)

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<sup>15</sup>M. Capek et al. "Acceleration Techniques in Matlab for EM Community". In: *Proceedings of the 7th European Conference on Antennas and Propagation (EUCAP)*. Gothenburg, Sweden, 2013

# Design of optimal antenna

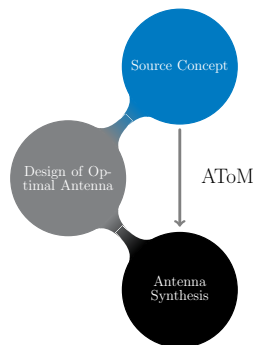


- ▶ The source concept was recently utilized for so-called optimal antenna design.
  - see e.g. recent papers by M. Cismasu and M. Gustafsson<sup>16</sup> or by J. Ethier and D. McNamara<sup>17</sup>
- ▶ To this purpose, it is beneficial to have a fast prototyping environment with partially open-source code.

<sup>16</sup>M. Cismasu and M. Gustafsson. “Antenna Bandwidth Optimization With Single Frequency Simulation”. In: *IEEE Trans. Antennas Propag.* 62.3 (2014), pp. 1304–1311

<sup>17</sup>J. L. T. Ethier and D. A. McNamara. “Antenna Shape Synthesis without Prior Specification of the Feedpoint Locations”. In: *IEEE Trans. Antennas Propag.* PP.99 (2014), p. 1. DOI: 0.1109/TAP.2014.2344107

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The optimal antenna design leads at least to a partial antenna synthesis!

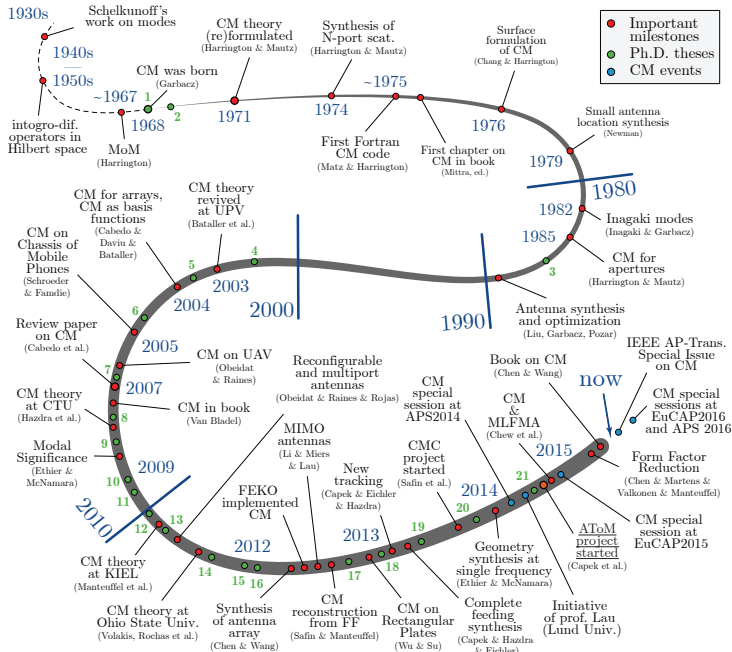
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# Characteristic mode decomposition



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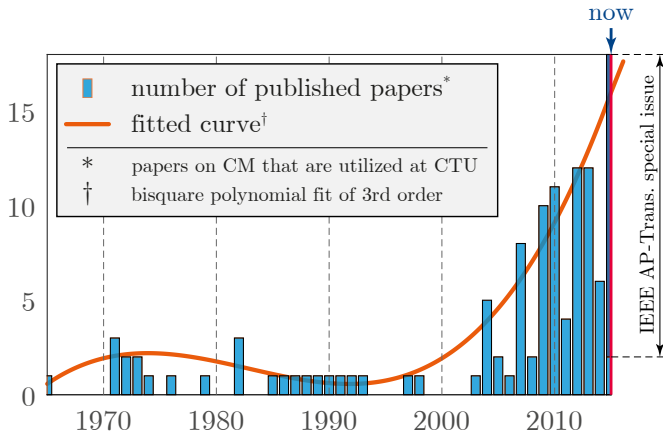




## Are CMs nowadays a hype?

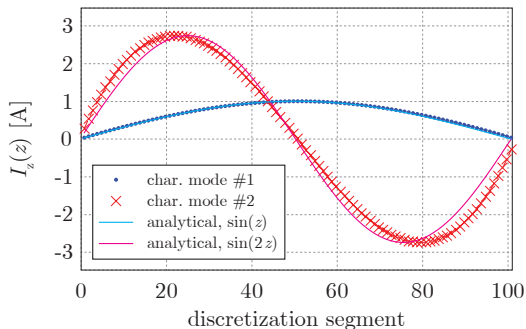


$$\chi J = \lambda \mathcal{R} J$$



Number of journal papers which are used at CTU to CM development.

# CM theory

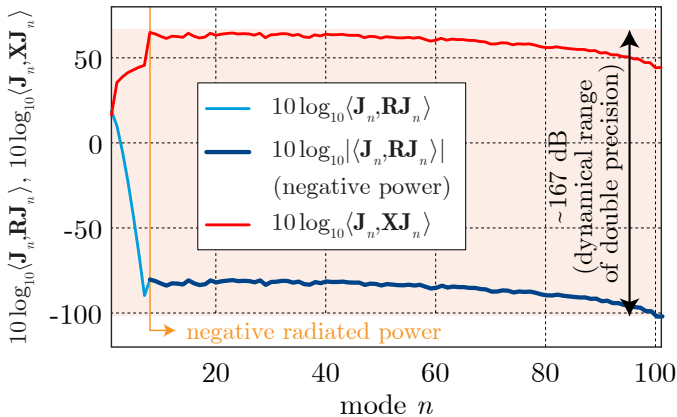


Comparison of CMs and sine basis.

- ▶ quite sensitive to non-symmetry of  $\mathcal{R}$ ,  $\mathcal{X}$ 
  - e.g. problem for Makarov's code
  - $\mathbf{A} = \frac{1}{2} (\mathbf{A} + \mathbf{A}^T)$ ,  $\mathbf{A} \in \mathbb{R}^{N \times N}$  seems useless
- ▶ tracking problems (discussed below)

- ▶ *natural* basis for radiating problems
- ▶ forms complete basis for any planar radiator
- ▶ ill-posed GEP (generalized eigen-value problem)
  - mainly because of  $\mathcal{R}$
  - some eigen-values are negative!

# CM and numerical precision



CM decomposition – numerical dynamics.

# CM practice



- ▶ alternatives
  - SEM modes
  - $\mathcal{X}\mathbf{J} = \kappa\mathbf{J}$
  - Inagaki modes<sup>18</sup>
- ▶ commercial software
  - FEKO
  - CST (2015)
  - WIPL-D (?)
  - CNC (in-house)
- ▶ challenges
  - potential utilization of periodic bound. cond. for CM
  - electrically large structures<sup>19</sup>
  - theory related to the CM
  - tracking

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<sup>18</sup>D. Liu. “Some Relationships Between Characteristic Modes and Inagaki Modes for Use in Scattering and Radiation Problems”. *PhD thesis. The Ohio State Univ., 1986*

<sup>19</sup>Q. I. Dai et al. “Multilevel Fast Multipole Algorithm for Characteristic Mode Analysis”. *In: (2014)*. URL: <http://arxiv.org/abs/1412.1756v2>

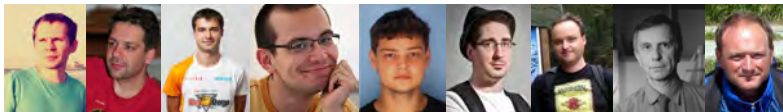
# About AToM



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# Project Details #1

- ▶ 3 participants:
  - CTU in Prague, BUT, MECAS ESI (subsidiary of ESI Group)
- ▶ project's staff (from left to right)
  - Miloslav Capek, Pavel Hazdra, Petr Kadlec, Vladimir Sedenka, Viktor Adler, Filip Kozak, Jaroslav Rymus, Milos Mazanek, Zbynek Raida



- ▶ students (from left to right)
  - Martin Marek, Ondrej Kratky, Vit Losenicky, Lukas Pospisil



## Project Details #2



- ▶ **antennatoolbox.com**
  - source concept<sup>20</sup> (charact. modes, optimization, post-processing)
  - various techniques to evaluate stored energy will be available
- ▶ all in **Matlab**
- ▶ **YouTube** channel
  - AToM's core is almost complete
  - numerical methods (MoM, BEM, CM) are now implemented

<sup>20</sup>See also the presentations from COST VISTA meetings in Madrid and Nice.

# Project Details #3



- ▶ application to become Matlab Pre-product Partner submitted



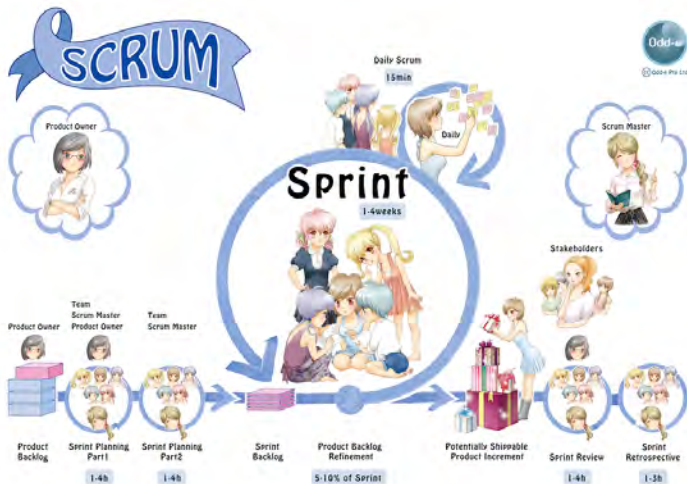
- however not yet approved...
- ▶ partially open-source code
  - key parts will be compiled (.p-code or .mex)
  - new functionality can easily be added by the users
  - detailed documentation of all features
- ▶ data storage: HDF5 – own I/O solution
- ▶ support of Technology Agency of the Czech Republic
  - 07/2014 – 12/2017
  - approx. 600 k€



$\alpha$ –projects logo of Technology Agency of Czech Republic.

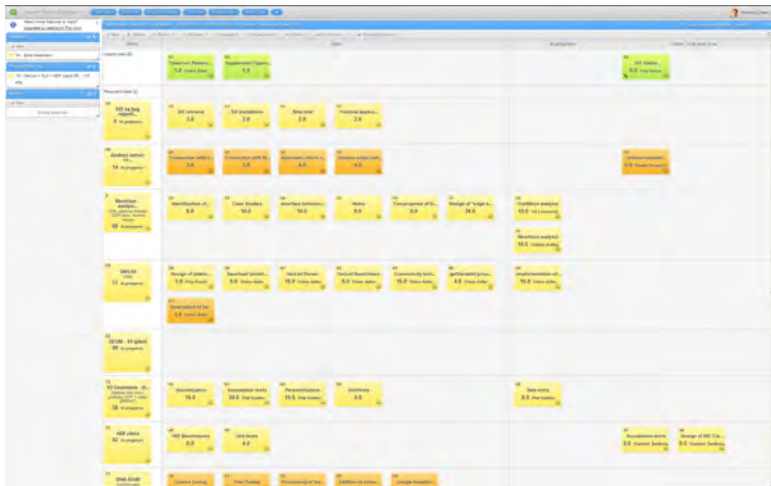


# Project's infrastructure – SCRUM



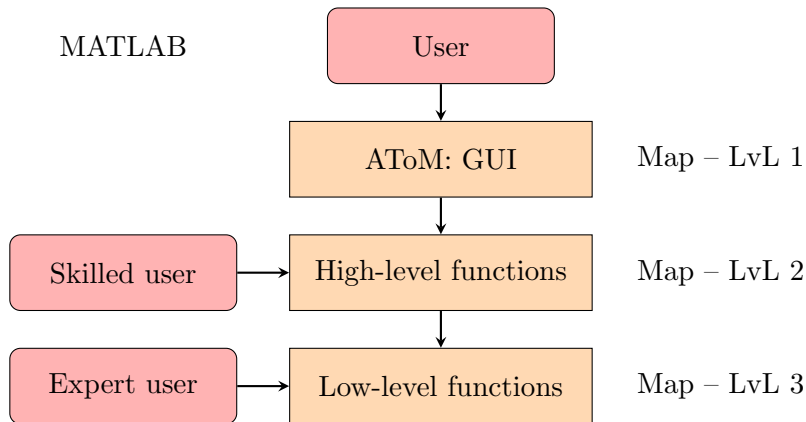
SCRUM – iterative and incremental agile SW development.

# Project's infrastructure – iceSCRUM



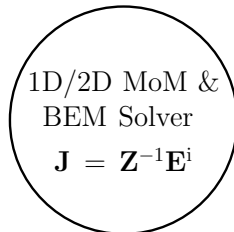
Open-source iceSCRUM software for Scrum methodology.

# Matlab-like Conception



Scheme of AToM – completely written in OOP.

Structure of AToM:

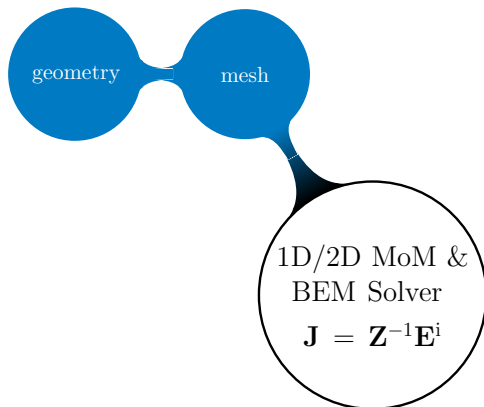


AToM – block diagram

# Complete EM Software



Structure of AToM:

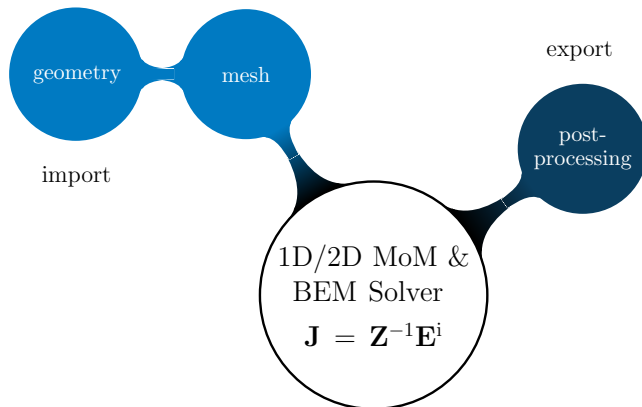


AToM – block diagram

# Complete EM Software



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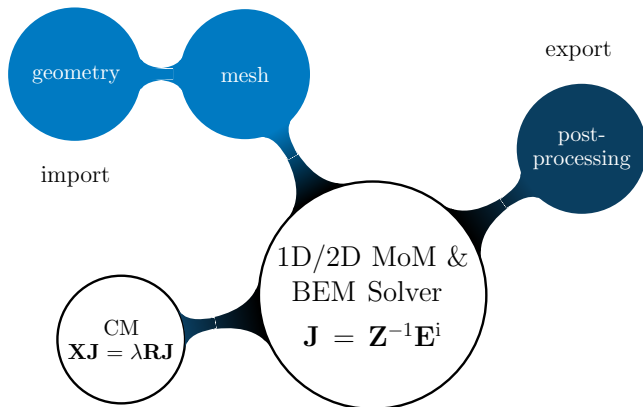


AToM – block diagram

# Complete EM Software



Structure of AToM:



AToM – block diagram

# Features of Matlab (R2015b)

Did you know?



- ▶ Run-time Type Analysis (>Matlab 6.5)
  - data types in m-file are noticed during the first run
- ▶ Just-In-Time-Accelerator<sup>21</sup>
  - parts of code that satisfy certain conditions are precompiled
- ▶ Object-oriented programming (>R2008)
  - surprisingly rich OOP (all classical OOP patterns feasible)
  - still under development
  - starts to be integrated everywhere (see e.g. in graphics in >R2014a)
- ▶ unitTest framework (>2014b)
  - GIT, SVN
- ▶ Source Control Integration
  - e.g. Jenkins can be utilized (see later)
- ▶ profiling via **profile**
  - JIT however deactivated during the **profile** measurement

<sup>21</sup>See [http://www.ee.columbia.edu/~marios/matlab/accel\\_matlab.pdf](http://www.ee.columbia.edu/~marios/matlab/accel_matlab.pdf).



# OOP & vectorization

```

1  % ...
2  % check whos weight is even number
3  function val = isWeightEven(objs)
4      val = mod([objs.weight],2) == 0;
5  end
6
7  % return "object" who is the oldest one...
8  function oldest_obj = whoIsTheOldest(objs)
9      allAges = [objs.age]; % for acceleration purposes
10     oldest_obj = objs(allAges == max(allAges));
11 end
12
13 % increase age of all objects
14 function objs = increaseAge(objs, incr_age)
15     [objs.age] = indexing.listEntries([objs.age] + incr_age);
16 end
17 % ...

```

```

1  % increase age (modification) – FOR approach
2  for thisObj = 1:N(thisN)
3      ppl(thisObj).increaseAge(10);
4  end

```

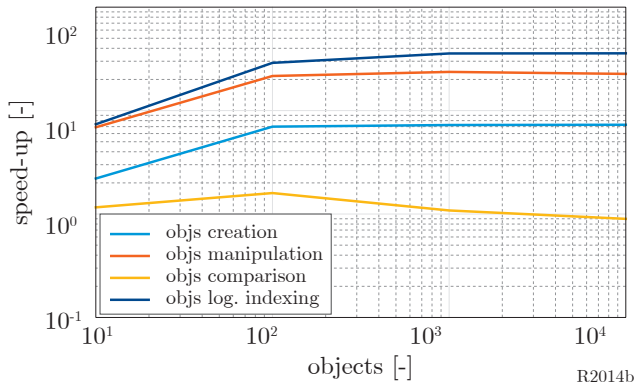
```

1  % increase age (modification) – vectorized approach
2  ppl.increaseAge(10);

```

OOP and vectorization (highest *level of abstraction* in Matlab).

# OOP: for $\times$ vectorization

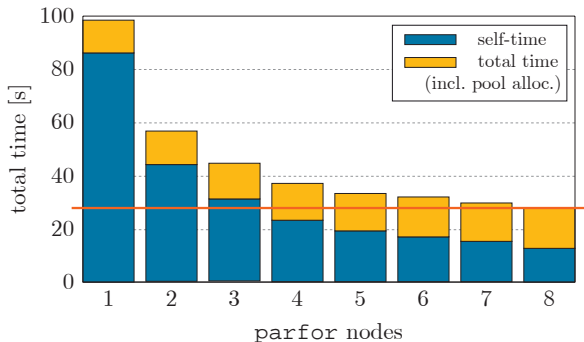


Full OOP code – comparison of `for` and vectorization, warp-up runs skipped, R2014b.

- ▶ the speed-up is 150–200% higher in R2015b

# GEP (CM): (naive) parallel solver

- ▶ e.g. CM cannot easily be accelerated on GPU



- ▶ beware of Amdahl's law<sup>22</sup>

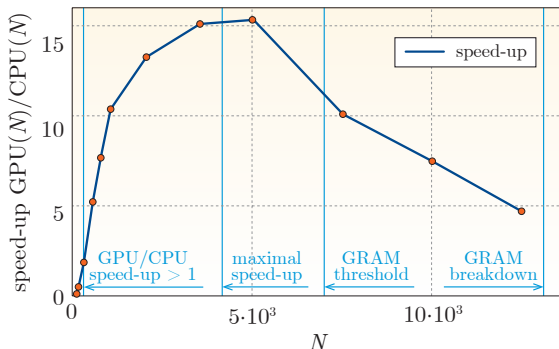
$$S(p, \tau_s) \leq \frac{1}{\tau_s + \frac{1-\tau_s}{p}}$$

CM decomposition parallelized on CPU in Matlab.

<sup>22</sup>T. Larsen. *Parallel High Performance Computing (With Emphasis Jacket Based GPU Computing)*. Aalborg University. 2011

# Bilinear forms: CPU $\times$ GPU

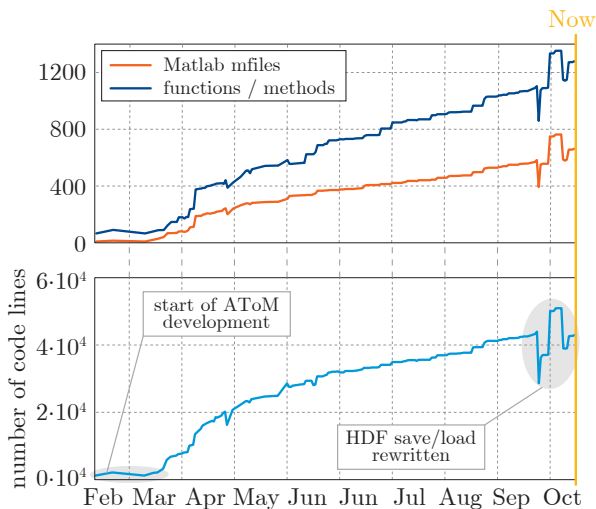
- Matlab R2013a, Jacket + `bsxfun`, GPU card: GTX580



Integration of radiated power as a function of current density discretized into  $N$  segments.

$$\text{Pr} = \frac{1}{8\pi\omega\epsilon} \int_{V_1} \int_{V_2} (k^2 \mathbf{J}(\mathbf{r}_1) \cdot \mathbf{J}(\mathbf{r}_2) - \nabla_1 \cdot \mathbf{J}(\mathbf{r}_1) \nabla_2 \cdot \mathbf{J}(\mathbf{r}_2)) \frac{\sin(kR)}{R} dV_2 dV_1$$

# AToM development – Where we are now?



directories	43
packages	61
classes	89
m-files	676
functions	1296
unitTests	1014
lines of code	43841
comments	4543

Valid data on 11/11/15, 1:37AM.

- ▶ data analysed daily at GIT server by Jenkins

AToM's statistics – aim at well-balanced development.

# AToM History and Workspace



- ▶ all actions in AToM are captured (`subsref` overloaded)
  - can be saved as m-file (and modified)
  - full control, can be evaluated as batch
- ▶ AToM has own Workspace
  - numerical values can be entered as variables
  - external function can be called to set up particular value
- ▶ code-GUI approach like in FEMlab<sup>23</sup> but better than FEMlam

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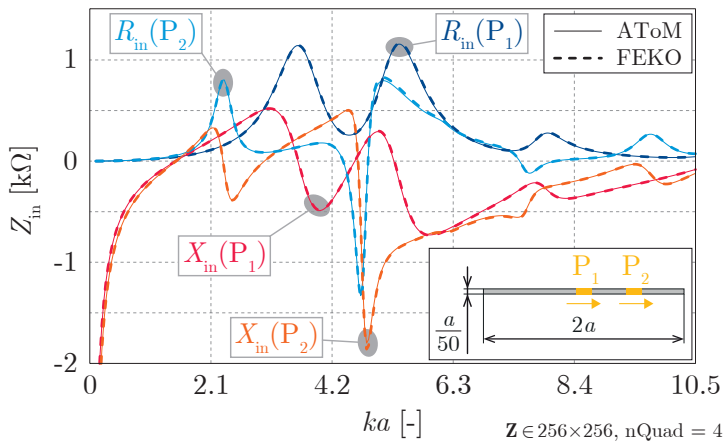
<sup>23</sup>Former Matlab toolbox, now Comsol Multiphysics.

# AToM History and Workspace



One of videos from our YouTube channel.

## AToM 2D-3D EFIE MoM (Matlab)



Preliminary results for simple structure (comparison with FEKO).

► multiple feeders

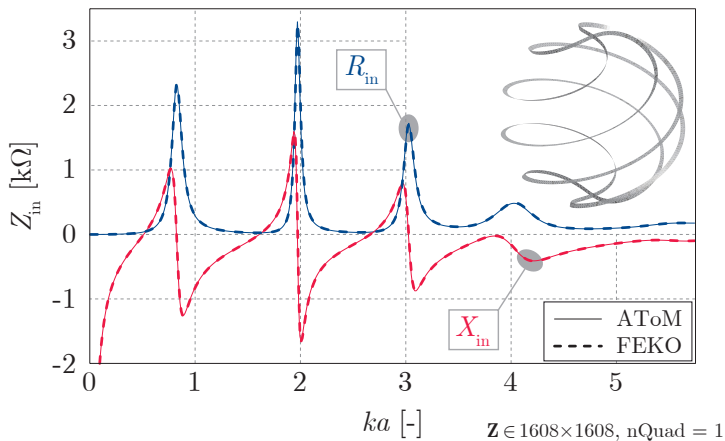


# AToM DesignViewer



Presentation of already generated spherical helix in AToM DesignViewer.

# Four voltage gaps & RWG junctions



Preliminary results for more complex structure (comparison with FEKO).

- multiple feeders, 3D surface, junctions

# Computational times – Comparison



- ▶ the same helix has been calculated both in FEKO and AToM
  - same discretization
  - same number of frequency samples (500)
  - same feeding model

# Computational times – Comparison



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  - same feeding model

	total time [s]
FEKO <sup>24</sup>	7302
Makarov <sup>25</sup>	998
AToM <sup>26</sup> (nQuad = 1)	
AToM <sup>26</sup> (nQuad = 2)	

... and the computational time of AToM?

<sup>24</sup>Parallel FEKO has been enabled.

<sup>25</sup>S. N. Makarov. *Antenna and EM Modeling with Matlab*. John Wiley, 2002

# Computational times – Comparison



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FEKO <sup>24</sup>	7302
Makarov <sup>25</sup>	998
AToM <sup>26</sup> (nQuad = 1)	933
AToM <sup>26</sup> (nQuad = 2)	1832

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<sup>24</sup>Parallel FEKO has been enabled.

<sup>25</sup>S. N. Makarov. *Antenna and EM Modeling with Matlab*. John Wiley, 2002

<sup>26</sup>Implicit Matlab parallelization heavily utilized.



# CM decomposition

- ▶ we utilize generalized Schur decomposition<sup>27</sup> (**eig**)
- ▶ iteratively restarted Arnoldi<sup>27</sup> will be implemented (**eigs**)
- ▶ powerful tracking<sup>28</sup> (heuristic approach)
  - still can be improved (Pearson formula<sup>29</sup>, far-field correlation<sup>30</sup>)
- ▶ modal quantities<sup>31</sup> ( $W_m^{u,v}$ ,  $W_e^{u,v}$ ,  $W_{rad}^{u,v}$ ,  $P_r^{u,v}$ ,  $D^{u,v}$ ,  $\eta_{rad}^{u,v}$ )
  - all quantities, except radiated power, have cross-terms!

$$\beta_{u,v} = \frac{\langle \mathbf{J}_u, \mathbf{E}_i \rangle \langle \mathbf{J}_v, \mathbf{E}_i \rangle (1 + \lambda_u \lambda_v)}{(1 + \lambda_u^2)(1 + \lambda_v^2)}, \quad A = \beta : \mathbf{A}_{\text{modal}} \quad (3)$$

<sup>24</sup>J. H. Wilkinson. *The Algebraic Eigenvalue Problem*. Oxford University Press, 1988

<sup>28</sup>M. Capek et al. “A Method for Tracking Characteristic Numbers and Vectors”. In: *Progress In Electromagnetics Research B* 33 (2011), pp. 115–134. DOI: 10.2528/PIERB11060209

<sup>29</sup>D. J. Ludick, U. Jakobus, and M. Vogel. “A Tracking Algorithm for the Eigenvectors Calculated with Characteristic Mode Analysis”. In: *Proceedings of the 8th European Conference on Antennas and Propagation (EUCAP)*. 2014, pp. 629–632

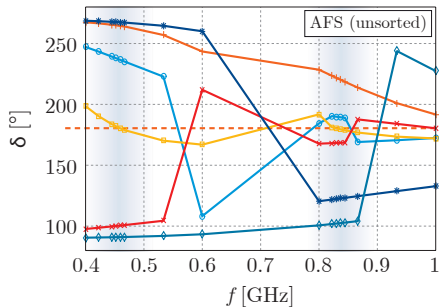
<sup>30</sup>Z. Miers and B. K. Lau. “Wide Band Characteristic Mode Tracking Utilizing Far-Field Patterns”. In: *IEEE Antennas Wireless Propag. Lett.* 14 (2015), pp. 1658–1661. DOI: 10.1109/LAWP.2015.2417351

<sup>4</sup>M. Capek, P. Hazdra, and J. Eichler. “A Method for the Evaluation of Radiation Q Based On Modal Approach”. In: *IEEE Trans. Antennas Propag.* 60.10 (2012;), pp. 4556–4567. DOI: 10.1109/TAP.2012.2207329



# Adaptive solver

- ▶ adaptive frequency solver (parallelized)
  - we are often interested in results around resonant frequency
  - improvement of tracking
  - acceleration of CM calculation

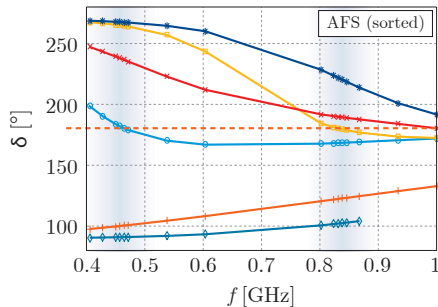
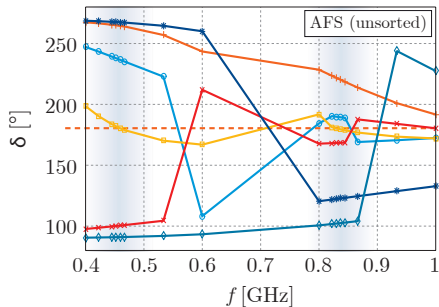


AFS after 3 iterations, raw data (left), rectangular plate  $30 \times 20$  cm.



# Adaptive solver

- ▶ adaptive frequency solver (parallelized)
  - we are often interested in results around resonant frequency
  - improvement of tracking
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AFS after 3 iterations, raw data (left), sorted data (right), rectangular plate 30 × 20 cm.





# FOPS: Fast Optimization Routines

We dispose of in-house

- ▶ SOO algorithms
  - Nelder-Mead, PSO, SOMA, GA
- ▶ MOO algorithms
  - PSO, SOMA
  - GA is implemented now
- ▶ hybrids<sup>32</sup>
  - e.g. Nelder-Mead + PSO (combination of global and fast local optimizers)

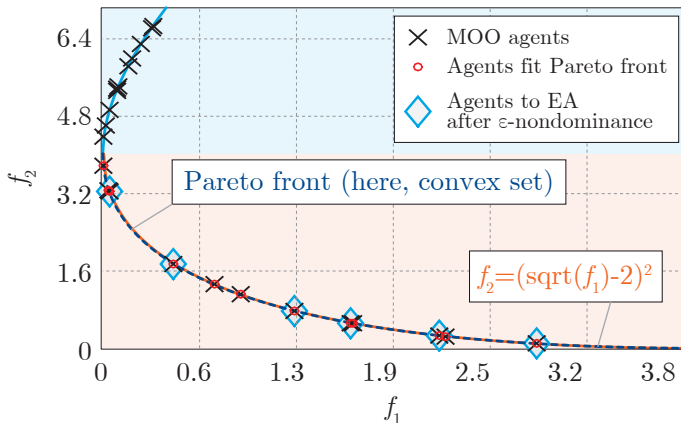
$$\begin{aligned}
 v_n^i &= (w_i + c_0 \text{rand}_n v_n^{i-1}) \\
 &+ c_1 \text{rand}_n (p_{\text{best},k} - v_n^{i-1}) + c_2 \text{rnd}_n (g_{\text{best},n} - x_n^{i-1}) \\
 &+ c_3 \text{rand}_n (g_{\text{NMbest},n} - x_n^{i-1})
 \end{aligned}$$

- ▶ all optimizers has general input

---

<sup>24</sup>D. H. Wolpert and W. G. Macready. “No Free Lunch Theorems for Optimization”. In: *IEEE Trans. Evolut. Comp.* 1.1 (1997), pp. 67–82. DOI: [10.1109/4235.585893](https://doi.org/10.1109/4235.585893)

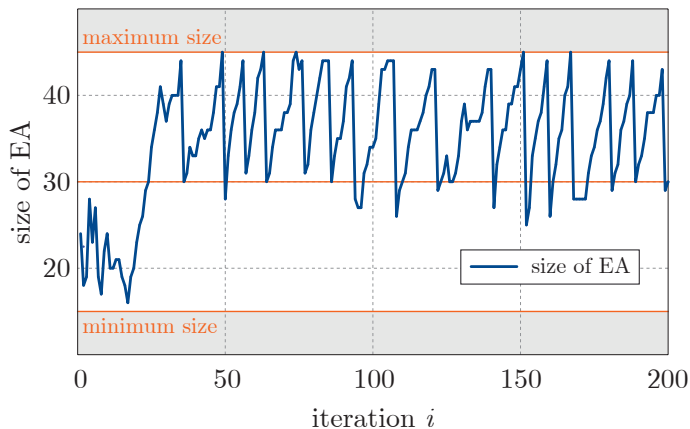
# MOO – selection of agent at the front



$\epsilon$ -nondominated solution for Schaffer's 1st problem<sup>33</sup>.

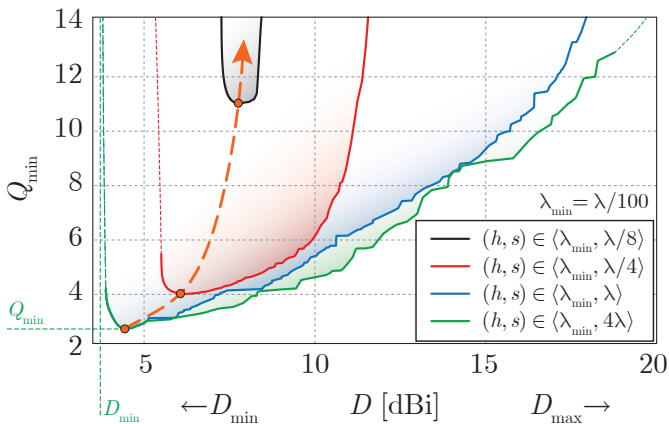
<sup>24</sup>K. Deb. *Multi-Objective Optimization using Evolutionary Algorithms*. John Wiley, 2001

# MOO – maintenance of the archive



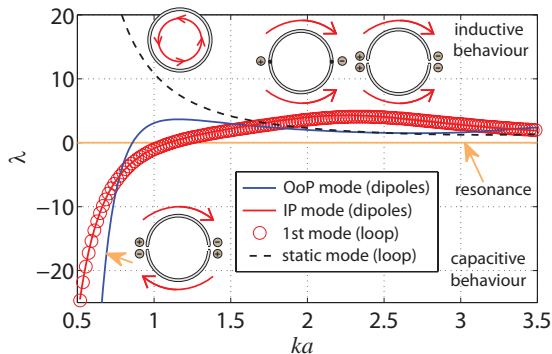
Adaptive maintenance of the external archive for Viennet's 1st problem, 50 agents.

## Example of MOO utilization – 4 dipoles



Two dipoles separated by distance  $s$  and placed  $h$  above PEC plane.

# Contemporary Techniques #1



Eigennumbers of two dipoles and the loop.

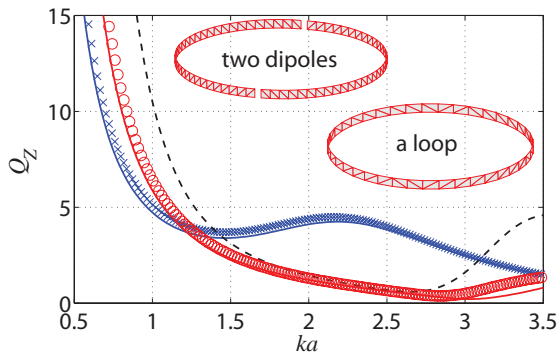
Modal decomposition  
and current's  
modifications

- ▶ characteristic modes<sup>34</sup> (QZ algorithm, Arnoldi)
- ▶ advanced tracking<sup>35</sup>

<sup>34</sup>M. Capek et al. "Implementation of the Theory of Characteristic Modes in Matlab". In: *IEEE Antennas Propag. Magazine* 55.2 (2013), pp. 176–189. DOI: 10.1109/MAP.2013.6529342

<sup>35</sup>M. Capek et al. "A Method for Tracking Characteristic Numbers and Vectors". In: *Progress In Electromagnetics Research B* 33 (2011), pp. 115–134. DOI: 10.2528/PIERB11060209

# Contemporary Techniques #2



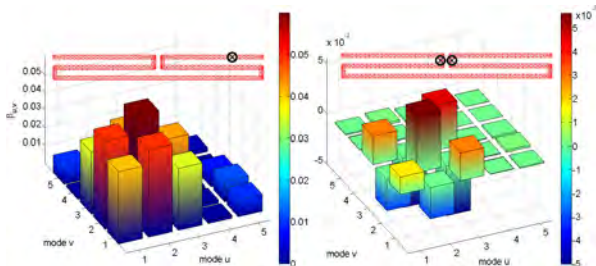
- × dipoles (IP)
- dipoles (OoP,  $\nabla \cdot \mathbf{J} \neq 0$ )
- dipoles (OoP,  $\nabla \cdot \mathbf{J} \equiv 0$ )
- loop – mode0 (static)
- loop – mode1

Equivalence of two topologically different structures.

Evaluation of  $Q_Z$  based on current densities

- ▶ so far, the best estimation of the  $Q$

# Contemporary Techniques #3



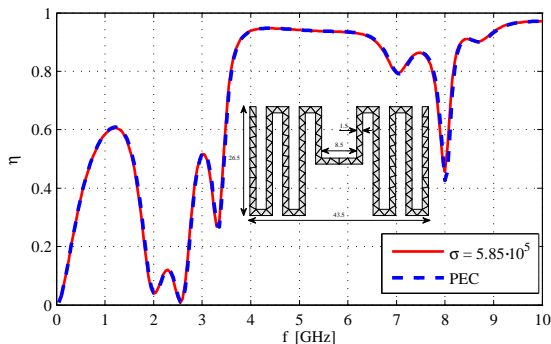
$\beta$  matrix before and after minimization of  $Q$ .

Utilization of characteristic modes for synthesis of feeding network<sup>36</sup>

- ▶ various goals:
  - minimization of  $Q$
  - desired rad. pattern
  - target input impedance

<sup>36</sup>M. Capek, P. Hazdra, and J. Eichler. "A Method for the Evaluation of Radiation Q Based On Modal Approach". In: *IEEE Trans. Antennas Propag.* 60.10 (2012;), pp. 4556–4567. doi: 10.1109/TAP.2012.2207329

# Contemporary Techniques #4



Radiation efficiency of a meandered dipole.

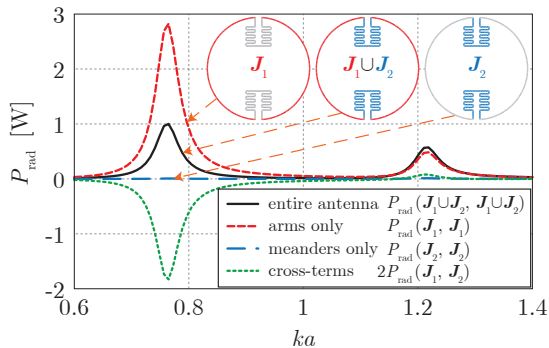
## Evaluation of radiation efficiency<sup>37</sup>

- ▶ approximation based on current flowing on PEC
- ▶ available even for modal currents
- ▶ excellent agreement with FEKO (IBC)

<sup>37</sup>M. Capek, J. Eichler, and P. Hazdra. "Evaluation of Radiation Efficiency from Characteristic Currents". In: *IET Microw. Antennas Propag.* 9.1 (2015), pp. 10–15. DOI: 10.1049/iet-map.2013.0473, M. Capek et al. "A Method for the Evaluation of Radiation Efficiency Based on Modal Approach". In: *Proceedings of the 8th European Conference on Antennas and Propagation (EUCAP)*. 2014



# Contemporary Techniques #5

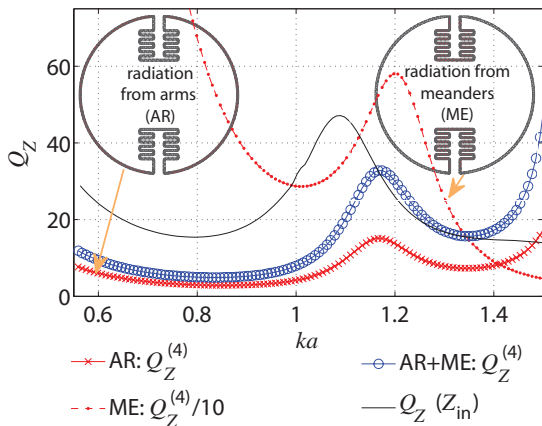


Structural decomposition

- what part of an antenna radiates well?

Structural decomposition of double U-notched antenna.

# Scheduled Features



Structural decomposition of U-notched antenna.

<sup>38</sup>M. Gustafsson, Ch. Sohl, and G. Kristensson. "Illustrations of New Physical Bounds on Linearly Polarized Antennas". In: *IEEE Trans. Antennas Propag.* 57.5 (2009), pp. 1319–1327. doi: 10.1109/TAP.2009.2016683

Of course, plenty of other features are scheduled:

- ▶ calculation of static polarizability<sup>38</sup>
- ▶ evaluation of the stored energy
- ▶ structural decomposition

# AToM → Visual Antenna

The key functionality of the AToM will be implemented into Visual Antenna package, developed by MECAS ESI company (subsidiary of ESI Group).

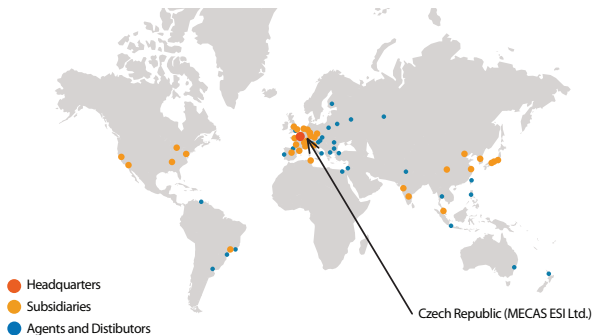
- ▶ Visual Antenna is a module for Visual CEM<sup>39</sup>, which integrates simulation tools for Computational Electromagnetics developed and distributed worldwide by ESI Group
- ▶ ESI offers complete solutions for End-to-End Virtual Prototyping



<sup>39</sup>ESI Group – Visual CEM. . URL:

<https://www.esi-group.com/software-services/virtual-environment/electromagnetics>

## ESI Group and MECAS ESI



- ▶ ESI Group<sup>40</sup> has more than 1000 employees, 15 subsidiaries, covers more than 40 countries and operates worldwide.

<sup>40</sup>We are happy that the whole project is supported by ESI Group and MECAS ESI company, since their support makes it possible to extent the up-to-date antenna techniques to the antenna designers.



Thank you!

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